

RESEARCH CENTRE FOR DATA ANALYTICS

# Scheduling Examples for Constraint Acquisition

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#### February 19, 2024



### **Overview**

- Why scheduling is a good field for Constraint Acquisition (CA)
- Present what scheduling problems looks like
- From simple to complex
- Give links to data in literature
- Show some realistic examples
- Focus on data, not algorithms



# Why Scheduling?

- This is the most successful application area for Constraint Programming (CP)
- Huge variety of different problem types and sub-types
- Often involves optimization of some objective(s)
- CP works best when there are many side constraints
  - Easy to add to a model
- There is a lot of literature
- Scheduling is important for many users



# Challenges

- Nearly always instances of different sizes
- Underlying problem is constantly evolving
  - New/deleted products, processes, machines
  - You need snapshot of relevant background data to reproduce results
- Nobody is interested in resolving previously solved instances
  - Unless you find better objective value
- There is rarely more than one solution kept for each instance
- Typically no non-solutions are produced and/or stored
- You may have different plans based on compromises between objectives/stakeholders



# Challenges (II)

- New instances are constantly added (every day)
  - We need to generate solutions for these unseen instances
- Big difference between planned schedule and actual, observed schedule
  - Machine break-downs
  - Quality issues, rework
  - Rush-orders, cancellations
  - Impact of (lack of) component stock
- Don't do as I do, do as I say
  - You don't want to learn the bad ways of fire-fighting
  - Hope that the original plan is stored, as well as the actual production data



# **Existing Literature**

- Methods to Learn Abstract Scheduling Models. Carchrae, Beck, Freuder. CP 2005. [9]
  - Suggests backdoor based approach to project scheduling
- Learning Scheduling Models from Event Data. Senderovich, Booth, Beck. ICAPS 2019. [40]
  - Learning models from traces of execution of actual schedules
- Guided Bottom-Up Interactive Constraint Acquisition. Tsouros, Berden, Guns. CP 2023. [42]
  - Example of smallish job-shop problem
- Boolean-Arithmetic Equations: Acquisition and Uses. Gindullin, Beldiceanu, Cheukam-Ngouonou, Douence, Quimper. CPAIOR 2023. [18]
  - Learning formulas from tables



### **My Interest**

- "Passive" Constraint Acquisition
  - Learn from positive (negative) examples
  - Few (one) solutions per instances, many instances
- Search for transferable model
  - Learn model from samples, apply to unseen instances
- Deal with large number of hidden variables
  - Stored results only show actionable decisions
- No membership queries for humans
  - Ask more meaningful questions: Can you interrupt execution of a task on this machine?
  - Automated oracles can only answer full queries



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ROADEF2022 ASSISTANT SE Use Case

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# **Examples from Books on CP**

- Can we acquire the models of scheduling problems in books on CP?
- Which books? There are books?



### **Books on CP**

Author	Title	Year	Pages	Language	CP System	Exercises
P Van Hentenryck	Constraint satisfaction in logic programming[20]	1989	224	English	CHIP[12]	-
F. Fages	Programmation logique par contraintes[13]	1996	192	French	GNU Prolog	yes
K. Marriott, P. Stuckey	Programming with Constraints[32]	1998	467	English	CLP(R)[27]	yes
P Van Hentenryck	The OPL Optimization Programming Language[21]	1999	254	English	OPL[22]	???
J. Hooker	Logic-Based Methods for Optimization[24]	2000	495	English	-	no
K. Apt	Principles of Constraint Programming[2]	2003	407	English	-	yes
R. Dechter	Constraint processing[11]	2003	481	English	-	???
T. Frühwirth, S. Abdennadher	Essentials of constraint programming[14]	2003	156	English	CHR	no
K. Apt, M. Wallace	Constraint Logic Programming using ECLiPSe [3]	2007	329	English	ECLiPSe[39]	yes
J. Hooker	Integrated Methods for Optimization[25]	2007	486	English	-	yes
P. Hofstedt, A. Wolf	Einführung in die Constraint- Programmierung[23]	2007	388	German	TURTLE[19] firstcs[44]	yes



# Books on CP (II)

Author	Title	Year	Pages	Language	CP System	Exercises
D. Poole, A. Mack- worth	Artificial Intelligence - Foundations of Computational Agents[35]	2010	900 (CSP ???)	English	-	yes
C. Lecoutre	Constraint Networks: Target- ing Simplicity for Techniques and Algorithms[30]	2013	320	English	???	???
A. Niederlinski	A Gentle Guide to Constraint Logic Programming via ECLiPSe[34]	2014	509	English	ECLiPSe[39]	yes
E. Tsang	Foundations of Constraint Satisfaction: The Classic Text[41]	2014	444	English	???	777
N. Zhou, H. Kjeller- strand. J. Fruhman	Constraint Solving and Planning with Picat[46]	2015	140	English	Picat[45]	yes
E. Bourreau, M. Gondran, P. La- comme, M. Vinot	De la programmation linéaire à la programmation par contraintes[7]	2019	348	French	Gusek CPLEX GLPK Choco[37]	no
E. Bourreau, M. Gondran, P. La- comme. M. Vinot	Programmation par Contraintes[8]	2020	232	French	Choco[37]	no
S. Russell, P. Norvig	Artificial Intelligence: A Modern Approach (4th Edition)[38]	2020	1115 (CSP 28)	English	-	no
M. Wallace	Building Decision Support Systems - using MiniZinc[43]	2020	224	English	MiniZinc[33]	yes

# Source: Workshop on Teaching Constraint Programming, Santanam, Simonis, 2023

- Tejas and myself are working on overview paper based on workshop
- Exists in draft form, if you are interested
- If you are teaching a CP course, please fill in
  - https://forms.gle/v54HUsbSXcyHmfME9
  - or contact us!

Survey	
Hellof We kindly ask for 5 minutes of your time for the following survey on 0 This information will be used for discussion: at the WTCP 2023 workshop is well as for general understanding on educational practices within the CP co	Toronto, as
helmut.simonis.eerk@gmail.com Switch account	Q
* Indicates required question	
Email *	
Your email	
Does your institution offer a CP course or a course that covers some around CP; SAT; or similar?	content
O Yes	
O No	
If no, what are the barriers or reasons?	
Your answer	
If your institution offers such a course, is there more than one course some aspect of this topic?	that covers
O Yes	
O No	
If you answered yes to the first question, who is the audience?	
O Undergraduates	
Graduate Students	



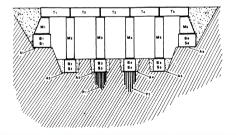
# Some Example Scheduling Problems

- Importance of data to acquire problem
- Constraint structure given as part of data, or implicit as part of problem structure
- Very often: data hardcoded in program
  - It saves space...
  - We should not teach this



# Bridge Scheduling Problem (Van Hentenryck 1989 [20])

- First scheduling problem with CHIP
- Based on PhD thesis of Bartusch
- Disjunctive Scheduling (RCPSP)
- Different types of temporal relations
- Minimize makespan



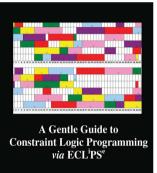
N	Name	description	duration	resource
1	PA	beginning of project	0	-
2	λ1	excavation (abutment 1)	4	excavator
3	A2	excavation (pillar 1)	2	excavator
4	A3	excavation (pillar 2)	2	excavator
5	A4	excavation (pillar 3)	2	excavator
6	A5	excavation (pillar 4)	2	excavator
7 1		excavation (abutment 2)	5	excavator
8	P1	foundation piles 2	20	pile-driver
9 1	P2	foundation piles 3	13	pile-driver
10	UE	erection of temporary housing	10	-
11	51	formwork (abutment 1)	8	carpentry
12	\$2	formwork (pillar 1)	4	carpentry
13		formwork (pillar 2)	4	carpentry
14	54	formwork (pillar 3)	4	carpentry
15	\$5	formwork (pillar 4)	4	carpentry
16	36	formwork (abutment 2)	10	carpentry
17	B1	concrete foundation (abutment 1)	1	concrete-mixes
18		concrete foundation (pillar 1)	ĩ	concrete-mixer
19	B3	concrete foundation (pillar 2)	ĩ	concrete-mixer
20		concrete foundation (pillar 3)	ī	concrete-mixes
21	85	concrete foundation (pillar 4)	ī	concrete-mixes
22		concrete foundation (abutment 2)	ī	concrete-mixe
23	AB1	concrete setting time (abutment 1)		-
24		concrete setting time (pillar 1)	ĩ	
25		concrete setting time (pillar 2)	ĩ	
26		concrete setting time (pillar 3)	ĩ	
27	AB5	concrete setting time (pillar 4)	ĩ	
28		concrete setting time (abutment 2)		
29		masonry work (abutment 1)	16	bricklaying
30		masonry work (pillar 1)	8	bricklaying
31		masonry work (pillar 2)	8	bricklaying
32		masonry work (pillar 3)	8	bricklaying
33		masonry work (pillar 4)	8	bricklaying
34	MG	masonry work (abutment 2)	20	bricklaying
35		delivery of the preformed bearers	2	crane
36	T1	positioning (preformed bearer 1)	12	crane
37		positioning (preformed bearer 2)	12	crane
38	73	positioning (preformed bearer 3)	12	crane
39	T4	positioning (preformed bearer 4)	12	crane
40	75	positioning (preformed bearer 5)	12	crane
41	UA	removal of the temporary housing	10	-
42	v1	filling 1	15	caterpillar
43		filling 2	10	caterpillar
44 1		point 1 of cost function	10	cacerpillar
45		point 1 of cost function	0	
46		end of project	0	
	***	end or brolede		-



**Teaching Exercises** 

# A Gentle Guide to Constraint Logic Programming (Niederlinski 2014 [34])

- Discusses many scheduling examples
- Most are open-coded, no separation of program and data
- ECLiPSe code given
- Result visualizations given



Antoni Niederliński

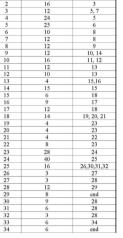
3-rd edition revised and



#### Teaching Exercises

### Ship Loading Example

/*9*/ /*10*/	LS :: 1400, LD :: 140,	Task	Man-hours
/*11*/	LD :: 140, LR :: 112,	1	12
/*12*/	End :: 1400,	2	16
/*13*/	Limit :: 112,	3	12
/*13*/	Limit :: 112,	4	24
/*14*/	cumulative(LS,LD,[R1,R2,R3,R4,R5,R6,R7],R8,R9,R10,R11,	5	25
/*14*/	R12,R13,R14,R15,R16,R17,R18,R19,R20,R21,R22,	6	10
	R23,R24,R25,R26,R27,R28,R29,R30,R31,R32,R33,R34],	7	12
	LF,Limit),	8	12
	LF,Limit),	9	12
/*15*/	S1 + D1 #=< S2.	10	16
/*15*/	S1 + D1 # = < S2, S1 + D1 # = < S4.	11	12
/*16*/	S1 + D1 #=< S4, S2 + D2 #=< S3.	12	10
		13	4
/*18*/	S3 + D3 #=< S5,	14	15
/*19*/	S3 + D3 #=< S7,	15	6
/*20*/	S4 + D4 #=< S5,	16	9
/*21*/	S5 + D5 #=< S6,	17	12
/*22*/	S6 + D6 #=< S8,	18	14
/*23*/	S7 + D7 #=< S8,	19	4
/*24*/	S8 + D8 #=< S9,	20	4
/*25*/	S9 + D9 #=< S10,	21	4
/*26*/	S9 + D9 #=< S14,	22	8
/*27*/	S10 + D10 #=< S11,	23	28
/*28*/	S10 + D10 #=< S12,	24	40
/*29*/	S11 + D11 #=< S13,	25	16
/*30*/	S12 + D12 #=< S13,	26	3
/*31*/	S13 + D13 #=< S15,	27	3
/*32*/	S13 + D13 #=< S16,	28	12
/*33*/	S14 + D14 #=< S15,	29	8
/*34*/	S15 + D15 #=< S18,	30	9
/*35*/	S16 + D16 #=< S17,	31	6
/*36*/	S17 + D17 #=< S18,	32	3
/*37*/	S18 + D18 #=< S19,	33	6
/*38*/	S18 + D18 #=< S20,	34	6



Next task 2,4



Teaching Exercises

# Job-Shop (Wallace, 2020 [43])

```
int: n machines:
int: n iobs:
int: n tasks = n machines:
set of int: jobs = 1... jobs:
set of int: tasks = 1..n tasks:
set of int: machines = 1..n machines :
array [jobs, tasks] of machines: jt machine:
array [jobs, tasks] of int: jt duration:
int: max end = 1050 :
array [jobs, tasks] of var 0.. max end: jt start:
var 0..max end: t end :
constraint
forall ( i in jobs. k in 1..(n tasks - 1) ) (
  it start[i, k] + it duration[i, k] <=</pre>
    jt_start[j, k + 1]
):
include "disjunctive.mzn" :
constraint
forall(m in machines)
  (disjunctive(
    [jt_start[j,t]|j in jobs,t in tasks where jt_machine[j,t]=m].
    [it duration[i.t]] in jobs. t in tasks where it machine[i.t]=m])
) :
```

solve minimize t\_end ;

n iobs = 10: n machines = 10: it machine = array2d(jobs, tasks, [0, 1, 2, 3, 4, 5, 6, 7, 8, 9]0. 2. 4. 9. 3. 1. 6. 5. 7. 8. 1. 0. 3. 2. 8. 5. 7. 6. 9. 4. 1, 2, 0, 4, 6, 8, 7, 3, 9, 5. 2. 0. 1. 5. 3. 4. 8. 7. 9. 6. 2. 1. 5. 3. 8. 9. 0. 6. 4. 7. 1. 0. 3. 2. 6. 5. 9. 8. 7. 4. 2. 0. 1. 5. 4. 6. 8. 9. 7. 3. 0. 1. 3. 5. 2. 9. 6. 7. 4. 8. 1. 0. 2. 6. 8. 9. 5. 3. 4. 7 1): it duration = arrav2d(iobs, tasks, [ 29, 78, 9, 36, 49, 11, 62, 56, 44, 21, 43, 90, 75, 11, 69, 28, 46, 46, 72, 30, 91. 85. 39. 74. 90. 10. 12. 89. 45. 33. 81, 95, 71, 99, 9, 52, 85, 98, 22, 43, 14. 6. 22. 61. 26. 69. 21. 49. 72. 53. 84. 2. 52. 95. 48. 72. 47. 65. 6. 25. 46. 37. 61. 13. 32. 21. 32. 89. 30. 55. 31, 86, 46, 74, 32, 88, 19, 48, 36, 79, 76. 69. 76. 51. 85. 11. 40. 89. 26. 74. 85, 13, 61, 7, 64, 76, 47, 52, 90, 45 1):



# Resource-Constrained Project Scheduling Problem (RCPSP) (Bourreau et al., 2019 [7])

- RCPSP with different approaches
- Different solvers, Choco-Solver, OPL Studio
- Complete Java projects
- Focus on modelling alternatives, performance
- Partial search (LDS)
- Also considers job-shop

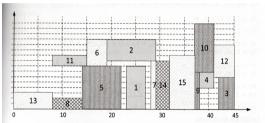


Figure 4-31. Solution optimale de valeur 45 obtenue avec la modélisation cumulative



### **Common Points**

- A good number of scheduling problems are presented
- Often not in a form that allows Constraint Acquisition to work
- Needs a lot of work to present data and solutions in machine readable form
- Resulting models are easy for tools to find, even with single (few) positive examples



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Literature Survey Papers with Data and (Solutions or Programs) Format Examples

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ROADEF2022 ASSISTANT SE Use Case

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### **Motivation**

- More and more papers attach data
- But, every paper uses different format
- CA ideally should be able to deal with these
- Broad basis for requirements analysis
- Most papers do not make it easy to understand data

# Methodology

- Use DBLP as primary source
- Extract relevant meta-data
- Text analysis of pdf to find shared concepts
- Manual extraction of some features

# **Existing Literature Surveys**

- Optimal methods for resource allocation and scheduling: a cross-disciplinary survey. Lombardi, Milano. 2012 [31].
  - Compares CP, MIP and hybrid methods
  - Gives examples of models and solution methods
  - From 2012, a lot of progress since then
- Applications of constraint programming in production scheduling problems: A descriptive bibliometric analysis. Prata, Abreu, and Nagano. 2024 [36].
  - Deeply flawed paper: data, methodology and analysis
  - Only focuses on flow/job/open shop



### Literature Survey - Recent Articles

#### Table 3: Articles from bibtex

Key	Authors	Title	LC	Cite	Year	Journal	Pages
PrataAN23 PrataAN23	Bruno A. Prata, Levi R. Abreu, Marcelo S. Nagano	Applications of constraint programming in production scheduling problems: A descriptive bibliometric analysis		[312]	2024	Results in Control and Optimization	1
abs-2402-00459 abs- 2402-00459	S. Nguyen, Dhananjay R. Thiruvady, Y. Sun, M. Zhang	Genetic-based Constraint Programming for Resource Constrained Job Scheduling		[279]	2024	CoRR	null
AbreuNP23 AbreuNP23	Levi Ribeiro de Abreu, Marcelo Seido Nagano, Bruno A. Prata	A new two-stage constraint programming approach for open shop scheduling problem with machine blocking	NO	[90]	2023	Int. J. Prod. Res.	20
AkramNHRSA23 AkramNHRSA23	Bilal Omar Akram, Nor Kamariah Noordin, F. Hashim, Mohd Fadlee A. Rasid, Mustafa Ismael Salman, Abdulrahman M. Abdulghani	Joint Scheduling and Routing Optimization for Deter- ministic Hybrid Traffic in Time-Sensitive Networks Using Constraint Programming		[7]	2023	IEEE Access	16
Caballero23 Caballero23	Jordi Coll Caballero	Scheduling through logic-based tools		[71]	2023	Constraints An Int. J.	1
GurPAE23 GurPAE23	S. Gür, M. Pinarbasi, Haci Mehmet Alakas, T. Eren	Operating room scheduling with surgical team: a new ap- proach with constraint programming and goal program- ming		[157]	2023	Central Eur. J. Oper. Res.	25
IsikYA23 IsikYA23	Eyüp Ensar Isik, Seyda Topaloglu Yildiz, Özge Satir Akpunar	Constraint programming models for the hybrid flow shop scheduling problem and its extensions		[186]	2023	Soft Comput.	28
LacknerMMWW23 LacknerMMWW23	M. Lackner, C. Mrkvicka, N. Musliu, D. Walkiewicz, F. Winter	Exact methods for the Oven Scheduling Problem		[224]	2023	Constraints An Int. J.	42
MontemanniD23 Monte- manniD23	R. Montemanni, M. Dell'Amico	Solving the Parallel Drone Scheduling Traveling Salesman Problem via Constraint Programming		[268]	2023	Algorithms	1
MontemanniD23a Mon- temanniD23a	R. Montemanni, M. Dell'Amico	Constraint programming models for the parallel drone scheduling vehicle routing problem		[267]	2023	EURO J. Comput. Op- tim.	1
ShaikhK23 ShaikhK23	Aftab Ahmed Shaikh, Abdullah Ayub Khan	Management of electronic ledger: a constraint program- ming approach for solving curricula scheduling problems	NO	[336]	2023	Int. J. Electron. Secur. Digit. Forensics	12
YuraszeckMCCR23 YuraszeckMCCR23	F. Yuraszeck, E. Montero, D. Canut-de-Bon, N. Cuneo, M. Rojel	A Constraint Programming Formulation of the Multi- Mode Resource-Constrained Project Scheduling Problem for the Flexible Job Shop Scheduling Problem		[406]	2023	IEEE Access	11
abs-2305-19888 abs- 2305-19888	V. Heinz, A. Novák, M. Vlk, Z. Hanzálek	Constraint Programming and Constructive Heuristics for Parallel Machine Scheduling with Sequence-Dependent Setups and Common Servers		[170]	2023	CoRR	null
abs-2306-05747 abs- 2306-05747	P. Tassel, M. Gebser, K. Schekotihin	An End-to-End Reinforcement Learning Approach for Job-Shop Scheduling Problems Based on Constraint Pro- gramming		[356]	2023	CoRR	null
abs-2312-13682 abs- 2312-13682	G. Perez, G. Glorian, W. Suijlen, A. Lallouet	A Constraint Programming Model for Scheduling the Un- loading of Trains in Ports: Extended		[300]	2023	CoRR	null
AbreuN22 AbreuN22	Levi Ribeiro de Abreu, Marcelo Seido Nagano	A new hybridization of adaptive large neighborhood search with constraint programming for open shop scheduling with sequence-dependent setup times		[89]	2022	Comput. Ind. Eng.	1
BourreauGGLT22 Bour- reauGGLT22	E. Bourreau, T. Garaix, M. Gondran, P. La- comme, N. Tchernev	A constraint-programming based decomposition method for the Generalised Workforce Scheduling and Routing Problem (GWSRP)	NO	[68]	2022	Int. J. Prod. Res.	19
CampeauG22 CampeauG22	L. Campeau, M. Gamache	Short- and medium-term optimization of underground mine planning using constraint programming		[72]	2022	Constraints An Int. J.	18
FetgoD22 FetgoD22	Sévérine Betmbe Fetgo, Clémentin Tayou Djamégni	Horizontally Elastic Edge-Finder Algorithm for Cumula- tive Resource Constraint Revisited		[116]	2022	Oper. Res. Forum	null
HeinzNVH22 HeinzNVH22	V. Heinz, A. Novák, M. Vlk, Z. Hanzálek	Constraint Programming and constructive heuristics for parallel machine scheduling with sequence-dependent se- tups and common servers		[169]	2022	Comput. Ind. Eng.	1

### Literature Survey - Extracted Concepts

Table 7: Keywords by Work and Domains

Work	Concepts	Classification	Constraints	ProgLanguages	CPSystems	Areas	Industries	Benchmarks	Algorithm
PrataAN23 [312]	scheduling, order, job, task, ac- tivity, resource, machine, preco- dence, preempt, sequence de- pendent setup, inventory, make span, completion time, flow span, completi	single ma- chine, parallel machine, Open Shop Scheduling Problem	cumulative, cir- cuit		СНІР	aircraft, robot, energy price, dairy	manufacturing industry	benchmark, real world, real life, http://, https://	time tabling
abs-2402-00459 [279]	scheduling, order, job, task, resource, machine, precedence, completion time, tardiness, ear- liness, job shop, due date, multi agent	single machine	cumulative, disjunctive, bin packing		or tools		mining industry	benchmark, generated in- stance, instance generator, real world, http://, https://, github	
AbreuNP23 [90] AkramNHRSA23 [7]	scheduling, order, task, resource, machine, preempt, completion time, distributed		bin packing	python	or tools	agriculture, medical		benchmark, https://	
Caballero23 [71]	scheduling, resource	RCPSP						http://, https://	
GurPAE23 [157]	scheduling, order, resource, ma- chine, inventory, distributed, re scheduling		cumulative		cplex	physician, nurse, patient, COVID		real life, https://	
IsikYA23 [186]	scheduling, order, job, task, resource, machine, precedence, preempt, sequence dependent setup, transportation, make span, cmax, completion time, tardiness, earliness, flow shop, job shop, release date, due date, setup time, distributed, batch process	single machine, parallel machine	cumulative, cir- cuit, nooverlap, endbeforestart		cplex, OPL	medical, robot	steel industry	benchmark, generated in- stance, real world, real life, http://, https://	energetic rea- soning
LacknerMMWW23 [224]	scheduling, order, job, task, ma- chine, make span, lateness, tardi- ness, earliness, job shop, release date, due date, setup time, batch process	single ma- chine, parallel machine, OSP	alternative constraint, cumulative, disjunctive, nooverlap, end- beforestart, bin packing		cplex, gurobi, or tools, OPL, cpo, chuffed, mini zinc	semiconductor, oven scheduling	electronics industry, man- ufacturing industry, steel industry	benchmark, instance genera- tor, random in- stance, real life, industrial part- ner, http://, https://, zon- odo	time tabling
MontemanniD23 [268]	scheduling, order, task, resource, machine, distributed		circuit	python	gurobi, or tools	robot		benchmark, supplemen- tary material, https://	
MontemanniD23a [267]	scheduling, order, task, trans- portation, completion time		circuit	python	or tools			benchmark, http://, https://	



### Literature Survey - Supplementary Materials

Table 4: Article Properties

Key	Title	CP System	Data Avail	Sol Avail	Code Avail	Based On	Classification	Constraints
PrataAN23 PrataAN23	Applications of constraint programming in production scheduling problems: A descriptive bibliometric analysis	-	-		-	-	survey	-
abs-2402-00459 abs- 2402-00459	Genetic-based Constraint Programming for Resource Constrained Job Scheduling	OR-Tools	у		n		RCJS	cumulatives
AbreuNP23 AbreuNP23	A new two-stage constraint programming approach for open shop scheduling problem with machine blocking	?	?		?	?	?	?
AkramNHRSA23 AkramNHRSA23	Joint Scheduling and Routing Optimization for Deter- ministic Hybrid Traffic in Time-Sensitive Networks Using Constraint Programming	OR-Tools	n		n		TSN	
Caballero23 Caballero23	Scheduling through logic-based tools	SAT	-		-	PhD Thesis	RCPSP	-
GurPAE23 GurPAE23	Operating room scheduling with surgical team: a new ap- proach with constraint programming and goal program- ming	Cplex	n		n	-	-	-
IsikYA23 IsikYA23	Constraint programming models for the hybrid flow shop scheduling problem and its extensions	OPL CP Opt	у		у	-	HFSP	alternative endBeforeStart noOverlap cumulative
LacknerMMWW23 LacknerMMWW23	Exact methods for the Oven Scheduling Problem	MiniZinc OPL	DZN JSON		у	[223]	OSP	alternative noOverlap forbidExtent
MontemanniD23 Monte- manniD23	Solving the Parallel Drone Scheduling Traveling Salesman Problem via Constraint Programming	OR-Tools	ref	У	n	-	PDSTSP	circuit
MontemanniD23a Mon- temanniD23a	Constraint programming models for the parallel drone scheduling vehicle routing problem	OR-Tools	ref		n		PDSTSP	circuit multipleCircuit
ShaikhK23 ShaikhK23	Management of electronic ledger: a constraint program- ming approach for solving curricula scheduling problems	?	?		?	?	?	?
YuraszeckMCCR23 YuraszeckMCCR23	A Constraint Programming Formulation of the Multi- Mode Resource-Constrained Project Scheduling Problem for the Flexible Job Shop Scheduling Problem	CP Opt	ref		n		FJSSP	alternative endBeforeStart cumulative
abs-2305-19888 abs- 2305-19888	Constraint Programming and Constructive Heuristics for Parallel Machine Scheduling with Sequence-Dependent Setups and Common Servers	CP Opt Gurobi	У	у	n		$P seq, ser C_{max}$	alternative noOverlap cumulative
abs-2306-05747 abs- 2306-05747	An End-to-End Reinforcement Learning Approach for Job-Shop Scheduling Problems Based on Constraint Pro- gramming	custom Choco	ref		n		JSSP	noOverlap
abs-2312-13682 abs- 2312-13682	A Constraint Programming Model for Scheduling the Un- loading of Trains in Ports: Extended	custom	n		n		SUTP	table disjunctive
AbreuN22 AbreuN22	A new hybridization of adaptive large neighborhood search with constraint programming for open shop scheduling with sequence-dependent setup times	Cplex CP Opt	у		n	-	OSSPST	noÖverlap
BourreauGGLT22 Bour- reauGGLT22	A constraint-programming based decomposition method for the Generalised Workforce Scheduling and Routing Problem (GWSRP)							
CampeauG22 CampeauG22	Short- and medium-term optimization of underground mine planning using constraint programming	CP Opt	ref		n			pulse alwaysIn endBeforeStart noOverlap
FetgoD22 FetgoD22	Horizontally Elastic Edge-Finder Algorithm for Curau'a- tive Resource Constraint Revisited							
HeinzNVH22	Constraint Programming and constructive heuristics for							

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# Literature Survey - The same for Papers

Table 2: Paper Properties

Key	Title	CP System	Data Avail	Sol Avail	Code Avail	Based On	Classification	Constraints
AalianPG23 AalianPG23	Optimization of Short-Term Underground Mine Planning Using Constraint Programming	CP Opt	n		n			7
Bit-Monnot23 Bit- Monnot23	Enhancing Hybrid CP-SAT Search for Disjunctive Scheduling	ARIES CP Opt OR-Tools Mistral	у		у	-	JSSP OSSP	-
EfthymiouY23 EfthymiouY23	Predicting the Optimal Period for Cyclic Hoist Scheduling Problems	OR-Tools	n		n	-	CHSP	-
JuvinHHL23 Juvin- HHL23	An Efficient Constraint Programming Approach to Pre- emptive Job Shop Scheduling	CP Opt Mistral	ref		У		PJSSP	endBeforeStart span noOverlap
JuvinHL23 JuvinHL23	Constraint Programming for the Robust Two-Machine Flow-Shop Scheduling Problem with Budgeted Uncer- tainty	CP Opt Cplex	ref		n		Perm FSSP	endBeforeStart noOverlap sameSequence
KameugneFND23 KameugneFND23	Horizontally Elastic Edge Finder Rule for Cumulative Constraint Based on Slack and Density	?	BL PSPlib		n	-	RCPSPs	cumulative
KimCMLLP23 KimCM- LLP23	Iterated Greedy Constraint Programming for Scheduling Steelmaking Continuous Casting	Gurobi OR-Tools	У		n	-	SCC	alternative noOverlap
Mehdizadeh-Somarin23 Mehdizadeh-Somarin23	A Constraint Programming Model for a Reconfigurable Job Shop Scheduling Problem with Machine Availability	CP Opt	n		n	1	JSSP RMS	alternative endBeforeStart noOverlap
PerezGSL23 PerezGSL23	A Constraint Programming Model for Scheduling the Un- loading of Trains in Ports	custom	n		n	-	SUTP	table disjunctive
PovedaAA23 PovedaAA23	Partially Preemptive Multi Skill/Mode Resource- Constrained Project Scheduling with Generalized Precedence Relations and Calendars	CP Opt MiniZinc Chuffed	у		У		PP-MS-MMRCPSP/max-cal	
SquillaciPR23 Squil- laciPR23	Scheduling Complex Observation Requests for a Con- stellation of Satellites: Large Neighborhood Search Ap- proaches	Cplex Studio	У		n	1	EOSP	?
TardivoDFMP23 Tardi- 70DFMP23	Constraint Propagation on GPU: A Case Study for the Cumulative Constraint	MiniCPP MiniZine	PSPLib BL Pack		У		RCPSP	cumulative
TasselGS23 TasselGS23	An End-to-End Reinforcement Learning Approach for Job-Shop Scheduling Problems Based on Constraint Pro- gramming	custom Choco	ref		У		JSSP	noOverlap
WangB23 WangB23	Dynamic All-Different and Maximal Cliques Constraints for Fixed Job Scheduling	FaCiLe	(y)		n	[390]	FJS	-
YuraszeckMC23 YuraszeckMC23	A competitive constraint programming approach for the group shop scheduling problem	CP Opt	ref		n	-	GSSP	noOverlap endBeforeStart
ArmstrongGOS22 Arm- strongGOS22	A Two-Phase Hybrid Approach for the Hybrid Flexible Flowshop with Transportation Times	CP Opt	(y)			[13]	$HFFm tt C_{max}$	endBeforeStart alternative cumulative noOverlap
3oudreaultSLQ22 3oudreaultSLQ22	A Constraint Programming Approach to Ship Refit Project Scheduling	MiniZinc Chuffed			У	1	RCPSP	cumulative
GeitzGSSW22 GeitzGSSW22	Solving the Extended Job Shop Scheduling Problem with AGVs - Classical and Quantum Approaches	firstCS OUBO	У		n	-	JSSP	
iFJZLL22 LiFJZLL22	Constraint Programming for a Novel Integrated Opti- mization of Blocking Job Shop Scheduling and Variable- Speed Transfer Robot Assignment	OPL CP Opt	ref		n	-	BJSSP	endBEforeStart alternative noOverlap
uelletQ22 OuelletQ22	A MinCumulative Resource Constraint	Giassed Sc	h <mark>e</mark> duling l		y	-		cumulative
DujanaAYB22 Ou- anaAYB22	Solving a realistic hybrid and flexible flow shop scheduling problem through constraint programming: industrial case	CP Opt	n		n	-	HFFS	minCumulative alternative span

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# **Literature Survey - Application Areas**

Table 8: Papers by Domain and Keyword

Domain	Keyword	High	Medium	Low
ApplicationAreas	crew scheduling	PourDERB18[308]	Mason01[259], Touraivane95[366]	WangB23[391], HeinzNVH22[169], HachemiGR11[158], BeldiceanuC02[42]
ApplicationAreas	dairies			Bartak02[33], Bartak02a[32]
ApplicationAreas	dairy	EscobetPQPRA19[110]	PrataAN23[312]	
ApplicationAreas	datacenter	HermenierDL11[174]		GalleguillosKSB19[124], Madi-WambaLOBM17[252], If- rimOS12[185], LetortBC12[228]
ApplicationAreas	datacentre			
ApplicationAreas	day ahead market			
ApplicationAreas	deep space			
ApplicationAreas	earth observation	SquillaciPR23[346], VerfaillieL01[375]	BensanaLV99[51]	PraletLJ15[311], SimoninAHL15[342], KelarevaTK13[197], Odd- iPCC03[288]
ApplicationAreas	earth orbit			SquillaciPR23[346]
ApplicationAreas	electroplating		RodosekW98[320]	EfthymiouY23[106], WallaceY20[389], NovasH12[286]
ApplicationAreas	energy price	GrimesIOS14[152], IfrimOS12[185]		PrataAN23[312], ÉscobetPQPRA19[110], BenediktŚMVH18[49], He0GLW18[161], LimHTB16[234]
ApplicationAreas	farming			WinterMMW22[396], Astrand0F21[20]
ApplicationAreas	forestry	HachemiGR11[158]		Astrand0F21[20]
ApplicationAreas	hoist	EfthymiouY23[106], WallaceY20[389], RodosekW98[320]	NovasH12[286], BonfiettiLBM11[61]	AstrandJZ18[21], BonfiettiLBM12[62], LombardiBMB11[242], KorbaaYG99[206], PapaB98[296]
ApplicationAreas	medical	ShinBBHO18[338], WangMD15[392], TopalogluO11[364]	HechingH16[163], DejemeppeD14[93], RendlPHPR12[318]	AkramNHRSA23[7], IsikYA23[186], AbreuN22[89], GeibingerKKIMMW21[133], FrimodigS19[121], Novas19[284], abs-1902-01193[8], GedikKEK18[132], BoothNB16[65], Doula- biRP14[103], Simonio7[344]
ApplicationAreas	nurse	GurPAE23[157], abs-1902-01193[8], ShinBBHO18[338], WangMD15[392], RendIPHPR12[318], Simonis07[344], Mason01[259]	OuelletQ22[291], GeibingerKKMMW21[133], GeibingerMM21[136], FrohnerTR19[122]	Derez (1232)290, abs-2312-13682[300], Frimodig S19[121], Nishikawa STT18a[281], Gedik KEK18[132], Doulabi RP14[103], Topaloglu O11[364]
ApplicationAreas	offshore	Interest [100]	SubulanC22[347]	BoudreaultSLQ22[67]
ApplicationAreas	oven scheduling	LacknerMMWW23[224], LacknerMMWW21[223]		
ApplicationAreas	patient	GurPAE23[157], FrimodigS19[121],	GeibingerKKMMW21[133]	MurinR19[273], DoulabiRP14[103], Simonis07[344]
		ShinBBHO18(338), HechingH16[163], WangMD15[392], DejemeppeD14[93], RendlPHPR12[318], TopalogluO11[364]	1	
ApplicationAreas	perfect square	BeldiceanuCDP11[43], BeldiceanuCP08[44]		
ApplicationAreas	physician	GeibingerKKMMW21[133], ShinBBHO18[338]		GurPAE23[157], FrimodigS19[121], WangMD15[392], TopalogluO11[364]
ApplicationAreas	pipeline	LopesCSM10[246], MouraSCL08[271], MouraSCL08a[270], ErtlK91[109]	BeniniBGM06[50], WolinskiKG04[399]	EfthymiouY23[106], PopovicCGNC22[307], HanenKP21[150], NishikawaST15[280], NishikawaST154[281], Labori- eRSV18[222], GilesH16[140], GoelSHFS15[144], Si- moninAHL15[342], NovasH10[285], BarlatCC08[31], Wolf03[397], KuchcinskW03[218], GruianK08[155], Darby- DowmanL497[86], SimonisC56[345]
ApplicationAreas	radiation therapy	FrimodigS19[121]		
ApplicationAreas	railway	PourDERB18[308], CappartS17[73], Acuna-AgostMFG09[4], AronssonBK09[15], Geske05[139], MartinPY01[258]	LaborieRSV18[222], Mason01[259]	BogaerdtW19[371], ZhouGL15[416], AbrilSB05[3], Wallace96[388]
ApplicationAreas	real time pricing	Contraction (1991)	He0GLW18[161], GrimesIOS14[152]	LimHTB16[234]
ApplicationAreas	rectangle packing	YangSS19[402]	interest in the second se	MossigeGSMC17[269], VilimLS15[385], BeldiceanuCDP11[43], SchuttW10[334], BeldiceanuCP08[44]



### **Literature Survey - Frequent Authors**

Table 5: Co-Authors of Articles/Papers

Author	Entries
Andreas Schutt	YangSS19[402] KreterSS17[217] YoungFS17[403] GoldwaserS17[146] SchuttS16[333] SzerediS16[351] KreterSS15[216] EvenSH15[111] EvenSH15a[112] Schut
	tFS13[330] cpaior-SchuttFS13[329] GuSS13[156] SchuttCSW12[328] SchuttFSW11[332] SchuttW10[334] SchuttFSW09[331]
Nicolas Beldiceanu	Madi-WambaLOBM17[252] Madi-WambaB16[251] LetortCB15[230] LetortCB13[229] LetortBC12[228] ClercqPBJ11[81] BeldiceanuCDP11[43] BeldiceanuCP08[44
	PoderB08[303] BeldiceanuP07[45] PoderBS04[304] BeldiceanuC02[42] AggounB92[5]
J. Christopher Beck	TangB20[352] BoothNB16[65] KoschB14[208] HeinzSB13[168] HeinzKB13[165] HeinzB12[164] KovacsB11[210] BeckFW11[38] WatsonB08[303] KovacsB08[205]
i chiniopher beek	CarchaeBF05[74] WuBB05[401] BeckDF97[37]
Emmanuel Hebrard	JuvinHHL23188 AntucriHHEN21[11] GodetLHS20[143] SimoninAHL15[342] SialaAH15[340] BessiereHMQW14[53] SimoninAHL12[341] BillautHL12[54]
Contraction recorders	GrimesH10[150] GrimesH10[149] GrimesH10[151] HebrardTW05[162]
Peter J. Stuckey	Granestri [159] Granestri [159] Granestri [159] Anterest [150] [150] [151]
Peter J. Stuckey	rangestry[adz] Dumirovics[6]00] Reference[217] senutro[6]350] Reference[216] BurtLPsis[70] Senutro[5]6[300] cpator-senutro[5]6[320] Guesta[100 Schutt/SW12]328 Schutt/SW01[332] Schutt/SW00[331]
Michele Lombardi	BonfiettiZLM16[64] LombardiBM15[241] BartoliniBBLM14[35] BonfiettiLM14[63] LombardiM12[245] BonfiettiLBM12[62] BonfiettiLBM11[61] LombardiBMB11[242 LombardiM10[244] LombardiBM02[243] HowerG8L07[373]
Pierre Lopez	
Pierre Lopez	JuvinHHL23[188] JuvinHHL23[189] Polo-MejiaALB20[306] NattafAL17[277] SimoninAHL15[342] NattafAL15[276] SimoninAHL12[341] BillautHL12[54]
	LahimerLH11[225] TrojetHL11[367] LopezAKYG00[247]
Michela Milano	BonfiettiZLM16[64] LombardiBM15[241] BartoliniBBLM14[35] BonfiettiLM14[63] LombardiM12[245] BonfiettiLBM12[62] BonfiettiLBM11[61] LombardiBMB11[242]
	LombardiM10[244] LombardiM09[243] HeniniBGM06[50]
Petr Vilím	LaborieRSV18[222] VilimLS15[385] Vilim11[382] Vilim09[380] cpaior-Vilim09[381] VilimBC05[384] Vilim05[379] VilimBC04[383] Vilim04[378] Vilim03[377]
	Vilim02[376]
Christian Artigues	PovedaÅA23[309] PohlAK22[305] Polo-MejiaALB20[306] NattafAL17[277] SimoninAHL15[342] NattafAL15[276] SialaAH15[340] SimoninAHL12[341] Ar
	tiguesBF04[16] ArtiguesR00[17]
John N. Hooker	Hooker17[181] HechingH16[163] CireCH13[80] CobanH10[82] Hooker06[180] Hooker05[178] cp-Hooker05[179] Hooker04[177] Hooker04[177]
Claude-Guy Quimper	BoudreaultSLQ22[67] OuelletQ22[291] Mercier-AubinGQ20[263] FahimiOQ18[113] KameugneFGOQ18[192] OuelletQ18[290] GingrasQ16[141] BessiereHMQW14[53]
ennare enj stamper	OutletO13[289]
Pierre Schaus	CappartS17[73] CauwelaertDMS16[76] DeiemeppeCS15[92] GavHLS15[128] GavHS15[129] cnaior-GavHS15[130] HoundiiSWD14[183] GavSS14[131] SchausHM
Forte Dennas	comparison of the second
Pascal Van Hentenryck	ColD11[350] FontaineMH16[117] EvenSH15[111] EvenSH15a[112] SchausHMCMD11[326] MonetteDH09[266] DoomsH08[102] HentenryckM08[173] HentenryckM04[172]
nacar ran mencentyer	DinchasH90101
Philippe Baptiste	BaptisteB18[26] Baptiste09[25] BaptisteLPN06[27] ArtiouchineB05[18] BaptisteP00[29] PapaB98[296] BaptisteP97[28] PapeB97[295]
Mats Carlsson	Daptisten 18/20/ Daptiste0/20/ Daptiste0_P/00/27/ AttionenneD00/18/ Daptister/0/29/ PapaD98/200/ Daptister/7/28/ PapeD97/295/ WesseneCS20/394/ MossingeGSMC17/260/ LetortCH15/220/ LetortCH13/229/ LetortBC12/28/ BeldiceanuCDP1143/ BeldiceanuCP08/44  BeldiceanuC02/42
Nysret Musliu	Wessene Calgary monoperator (1,20) Lenorto Dio (20) Le
Nysret Mushu	LacknerMMW w23[224] WinterMMW22[396] LacknerMMWW21[223] GeibingerKKMMW21[133] GeibingerMa121[136] GeibingerMa121[136] abs-1911-04706[134 KletzanderMI7[204]
Helmut Simonis	ArmstrongGOS22[14] ArmstrongGOS21[13] GrimesIOS14[152] IfrimOS12[185] Simonis07[344] SimonisC95[345] Simonis95[343] DincbasSH90[101]
Alessio Bonfietti	BonfiettiZLM16[64] fbonfietti16[60] LombardiBM15[241] BonfiettiLM14[63] BonfiettiLBM12[62] BonfiettiLBM11[61] LombardiBMB11[242]
Zdenek Hanzálek	Mehdizadeh-Somarin23[260] abs-2305-19888[170] HeinzŇVH22[169] VlkHT21[387] BenediktMH20[48] BenediktSMVH18[49] KelbelH11[198]
Philippe Laborie	LunardiBLRV20[249] LaborieRSV18[222] Laborie18a[221] MelgarejoLS15[6] VilimLS15[385] Laborie09[220] BaptisteLPN06[27]
Gabriela P. Henning	NovaraNH16[283] NovasH14[287] NovasH12[286] NovasH10[285] ZeballosQH10[409] ZeballosH05[408] QuirogaZH05[317]
Stefan Heinz	HeinzSB13[168] HeinzKB13[165] HeinzSSW12[166] HeinzB12[164] HeinzS11[167] BertholdHLMS10[52]
András Kovács	KovacsB11[210] KovacsK11[212] KovacsB08[209] KovacsV06[214] KovacsEKV05[211] KovacsV04[213]
Emmanuel Poder	BeldiceanuCDP11[43] abs-0907-0939[302] BeldiceanuCP08[44] PoderB08[303] BeldiceanuP07[45] PoderBS04[304]
Mark Wallace	WallaceY20[389] He0GLW18[161] SchuttFSW09[331] SakkoutW00[325] RodosekW98[320] Wallace96[388]
Roman Barták	BartakS11[34] VilimBC05[384] VilimBC04[383] Bartak02[33] Bartak02a[32]
Yves Deville	HoundiiSWD14[183] DelemeppeD14[93] SchausHMCMD11[326] MonetteD[09]266] MonetteDD07[265]
Thibaut Feydy	YoungFS17[403] SchuttFS13[330] epsior-SchuttFS13[329] SchuttFSW11[332] SchuttFSW09[331]
Roger Kameugne	KameugneFNJ231931 KameugneFGOQ18192 KameugneFSN14195 KameugneFSN11194
Claude Le Pape	BaptisteLPN6/271 BaptisteP00/291 PapaB58(296) BaptisteP07(28) PapeB7(295)
Juan M. Novas	Norval 9[284] NovaraNH 6[283] NovasH 14[287] NovasH 12[286] NovasH 10[285]
Louis-Martin Rousseau	Novas19[29] Novaravin10[263] Novasni 14[267] Novasni 12[269] Novasni 10[269] DoulabRP16[104] PesantRit[5]001 DoulabRP14[103] ChapadoaJR11[78] HachemiGR11[158]
André A. Ciré	CircCH13801 LopesCSM10[2461 MouraSCL08[271] MouraSCL08a[270]
Juca Benini	CireCritisBoj Lopex-5m10[246] atouraS-CL046[271] MontaS-CL046[240] BonfiettLBM1[262] BonfiettLBM1[261] LombardiBMB11[2428 [artin]BGM06[50]
Cyrille Dejemeppe	CauwelaertDMS16[76] Dejemeppe16[91] DejemeppeCS15[92] DejemeppeD14[93]
Steven Gay	GayHLS15[128] GayHS15[129] cpaior-GayHS15[130] GaySS14[131]
Tobias Geibinger	GeibingerKKMMW21[133] GeibingerMM21[136] GeibingerMM19[135] abs-1911-04766[134]
Diarmuid Grimes	GrimesIOS14[152] GrimesH11[150] GrimesH10[149] GrimesHM09[151]
Krzysztof Kuchcinski	WolinskiKG04[399] WolinskiKG04a[400] KuchcinskiW03[218] GruianK98[155]
Laurent Michel	TardivoDFMP23[354] SchausHMCMD11[326] HentenryckM08[173] HentenryckM04[172]
Florian Mischek	GeibingerKKMMW21[133] GeibingerMM21[136] GeibingerMM19[135] abs-1911-04766[134]

# Insight

# Most Recent Papers/Articles with Supplementary Materials

Key	Size	Instances	MetaData	Format	Solutions	Checker
AbreuN22 [10]	1.3MB	192	n	TS	n	n
AntuoriHHEN21 [1]	23.3MB	120	n	TS	n	n
ArmstrongGOS21 [4]	11MB	225	n	dzn	n	n
BenderWS21 [5]	116KB	84	У	ΤS	n	n
Bit-Monnot23 [6]	23.5MB	357	n	ΤS	n	n
GeibingerKKMMW21 [15]	40KB					n
GeibingerMM21 [16]	13.9MB					n
GeitzGSSW22 [17]	16.0KB					n
IsikYA23 [26]	3.9MB					n
KimCMLLP23 [28]	4.1MB					n
KovacsTKSG21 [29]	138MB	18	n	JSON	n	n



# AbreuN22 [10]

1	
2	MO
3	33 436 108
4	401 221 132
5	177 259 155
6	
7	м1
8	120 26 280
9	184 250 252
10	214 25 469
11	
12	м2
13	393 53 262
14	70 24 420
15	463 304 168
16	
17	



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# AntuoriHHEN21 [1]

1	49	2																				
2	80	00																				
3																						
4	0	0	0	PF	195	50	0	40	0	36	25	2										
5	1	0	0	DF	195	50	1	40	0	36	25	2										
6	2	0	0	PE	195	50	1	15	0	36	25	2										
7	3	0	0	DE	195	50	0	15	0	36	25	2										
8	4	0	1	PF	195	50	0	40	36	525	7:	250	2	2								
9	5	0	1	DF	195	50	1	40	36	25	7:	250	2	2								
10	6	0	1	PE	195	50	1	15	36	25	7:	250	2	2								
11	7	0	1	DE	195	50	0	15	36	525	7:	250	2	2								
12	8	0	2	PF	195	50	0	40	72	250	1	087	5	2								
13	9	0	2	$\mathbf{DF}$	195	50	1	40	72	250	1	087	5	2								
14	10	0	2	PE	19	95(	0 1	15	5 7	25	0 3	108	75	5 3	2							
15	11	0	2	DE	19	95(	D C	15	5 7	25	0	108	75	5 3	2							
16	12	0	З	PF	19	95(	D C	40	) 1	.08	75	14	50	00	2							
17	13	0	3	DF	19	95(	0 1	. 40	) 1	.08	75	14	50	00	2							
18	14	0	3	PE	19	95(	0 1	15	5 1	.08	75	14	50	00	2							
19	15	0	3	DE	19	95(	D C	15	5 1	.08	75	14	50	00	2							
20	16	0	4	PF	19	95(	D C	40	) 1	45	00	18	12	25	2							
21	17	0	4	DF	19	95(	0 1	. 40	) 1	45	00	18	12	25	2							
22	18	0	4	PE	19	95(	0 1	15	5 1	45	00	18	12	25	2							
23	19	0	4			95(				45		18			2							
24	20	0	5			95(				81		21			2							
25	21	0	5			95(				81	_	21			2							
26	22	0	5			95(				81		21			2							
27	23	0	5			95(			-	81:		21			2							
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29	25	0	6	DF	19	950	01	. 40	) 2	217	50	25	37	75	2						_	
g Liter	atıu	re.														In	S	C	1h	۱t.		
5 Enten	areu																	3	<b>7</b>		-	

CP Based Scheduling Literature

# ArmstrongGOS21 [4]

- Instances in MiniZinc .dzn format
- Single file per instance
- Matches program in paper
- Integers, String, Arrays, Sets
- Tedious to parse for other solvers
- Could now be replaced by JSON
- Checker is easy to add

```
% J&J flowshop data
T = 1...154:
P = 1...134:
M = 1...80*
S = 1...8:
tuples = 1..800;
1b = 62
ub = 63;
m = 801
duration=
[3, 10, 4, 4, 6, 8, 7, 4, 1, 4, 7, 10, 1, 4, 9, 9, 9, 3, 1, 1, 6, 8, 6, 8, 2, 3, 6, 6, 8
5.9.4.3.3.7.10.5.10.8.3.10.9.2.6.6.4.7.7.9.4.10.8.8.5.9.4.3
capacity = [10,10,10,10,10,10,10,10];
stage =
11.2.3.4.5.6.7.8.1.2.3.4.5.6.7.8.1.2.3.5.6.7.1.2.3.4.5.6.7.8
5, 6, 7, 8, 1, 2, 3, 4, 5, 6, 7, 8, 1, 2, 3, 4, 5, 6, 7, 8, 1, 2, 3, 4, 5, 6, 7, 8, 1, 2,
machines =
[(1, 2, 3, 4, 5, 6, 7, 8, 9, 10), (11, 12, 13, 14, 15, 16, 17, 18, 19, 20), (21,
.78.79.80).(1.2.3.4.5.6.7.8.9.10).(11.12.13.14.15.16.17.18.1
4.75.76.77.78.79.80). (1.2.3.4.5.6.7.8.9.10). (11.12.13.14.15.
(11, 12, 13, 14, 15, 16, 17, 18, 19, 20), (21, 22, 23, 24, 25, 26, 27, 28, 29,
7.8.9.101. (11.12.13.14.15.16.17.18.19.201. (21.22.23.24.25.26
2,3,4,5,6,7,8,9,10),(11,12,13,14,15,16,17,18,19,20),(21,22,2)
79.80), (1.2.3.4.5.6.7.8.9.10), (11.12.13.14.15.16.17.18.19.20
8, 9, 10), (11, 12, 13, 14, 15, 16, 17, 18, 19, 20), (21, 22, 23, 24, 25, 26, 2
5, 26, 27, 28, 29, 30}, (31, 32, 33, 34, 35, 36, 37, 38, 39, 40}, (41, 42, 43,
22,23,24,25,26,27,28,29,30},{31,32,33,34,35,36,37,38,39,40},
9,201, (21, 22, 23, 24, 25, 26, 27, 28, 29, 30), (41, 42, 43, 44, 45, 46, 47,
26, 27, 28, 29, 30), (31, 32, 33, 34, 35, 36, 37, 38, 39, 40), (41, 42, 43, 44
23, 24, 25, 26, 27, 28, 29, 30), (31, 32, 33, 34, 35, 36, 37, 38, 39, 40), (4
20}, (21, 22, 23, 24, 25, 26, 27, 28, 29, 30}, (31, 32, 33, 34, 35, 36, 37, 38
17.18.19.201.121.22.23.24.25.26.27.28.29.301.131.32.33.34.3
3.14.15.16.17.18.19.20).(21.22.23.24.25.26.27.28.29.30).(31.
}, {11, 12, 13, 14, 15, 16, 17, 18, 19, 20}, {21, 22, 23, 24, 25, 26, 27, 28, 2
6.7.8.9.10).(11.12.13.14.15.16.17.18.19.20).(21.22.23.24.25.
1,2,3,4,5,6,7,8,9,10},(11,12,13,14,15,16,17,18,19,20},(21,22
8.79.8011/
prec =
111.212.313.414.515.616.717.819.10110.11111.12112.13113.1411
9149,50150,51151,52152,53153,54155,56156,57157,58158,59159,6
4,95|95,96|96,97|97,98|99,100|100.101|101.102|102.103|103.10
1129.1301131.1321132.1331133.1341134.1351135.1361136.1371137
transportTime =
```

# BenderWS21 [5]

### • Describes format of data

1	4,2,4
2	64,43
3	30,30
4	0,186.454,228.75,116.595,175.71
5	3,2,2,3,2,2,2,3
6	27.5399,14.5452,44.6473,6.2793,2.5734
7	35.4074,25.5414,44.8147,10.3621,22.0405
8	



# Bit-Monnot23 [6]

- Mix of strings and numbers
- Text stream
- Different formats for job shop and open shop instances

```
nb jobs nb machines
      10 10 0 0 0 0
      Times
      88 68 94 99 67 89 77 99 86 92
      72 50 69 75 94 66 92 82
                              94 63
 6
      83 61 83 65 64 85 78 85 55 77
      94 68
            61 99 54 75 66 76 63 67
8
      69 88 82 95 99 67 95 68 67 86
9
      99 81 64 66 80 80 69 62 79 88
      50
         86
            97
               96 95 97 66 99 52 71
      98 73 82 51 71 94 85 62 95 79
      94 71 81 85 66 90 76 58 93 97
      50 59 82 67 56 96 58 81 59 96
14
      Machines
      597
            62310814
      6
          7
            5
              з
                912
                      8 10
      10
         9 1
             2
                7
                 6
                   8
                      5
                       3 4
      8
        3
          2
            5
                76
                      10 9
               4
      4
        5
          10
             9
                 3
                      6
                        8 2
      2
        5
          6
            7
               9
                з
                     10
                       4 1
          5
                  3 6
                       7 10
                Q
            з
                      9 10
                6
      17482356
                      9 10
24
      4 1 2 9 8 10 7 5 6 3
```



# KovacsTKSG21 [29]

- Nice JSON format of data
- Real-life data
- One instance per file, one file per instance
- Task length given as float
- Machine capacity given as float

```
"info": {
                              "days": 14,
                              "objective": {
                                "penaltyPerDay": 1,
                                "oneTimePenalty": 3.
                                "jobWeight": 1,
                                "projects": []
                            "tasks":
                                "id": 835789.
                                "machine": 846644.
                                "job": 972494.
                                "length": 46.085566752371655,
                                "earliest start": 0,
                                "directly after last": false.
                                "free days before": 0
                                "id": 708746.
                                "machine": 521987.
                                "job": 972494.
                                "length": 22,59964864783412.
                                "earliest start": 1,
                                "directly after last": false.
                                "free days before": 0
                                "id": 578563.
                                "machine": 908456.
                                "job": 972494,
CP Based Scheduli
                                "length": 0.09596492713072255.
                                "earliest start", 2
```

## Challenges

- Data formats are often ad-hoc, token streams common
- Meaning of value depends on position in stream
- Solutions very rarely provided
  - If given, only one (best) solution is given
  - Sometimes can be generated from code which is provided
- Checkers non-existent
- For many papers, extracting the constraint model is not the challenge
  - Finding a good solution quickly enough is



## **Table of Contents**

### **Teaching Exercises**

### CP Based Scheduling Literature

Literature Survey Papers with Data and (Solutions or Programs) Format Examples

### **Realistic Examples**

ROADEF2022 ASSISTANT SE Use Case

### Conclusion

### Bibliography



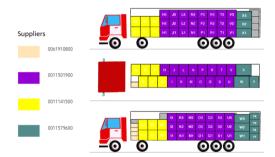
## **Realistic Examples**

- Two examples of a more complex nature
- Realistic, but not real problem set
- Show complexity of real-world problems



## Roadef2022 Challenge

- Competition by French OR society Roadef, European OR society Euro
- Problem provided by Renault
- Schedule transport of components from suppliers to factories
- Decide when to transport item, how to pack them into trucks
- Decide how many resources (trucks) are needed
- Not a vehicle routing problem (routes predefined and given)
- Objective Minimize cost (resources plus earliness cost of items)





## Input Data

### Potential Trucks

Supplier code; Supplier loading order; Supplier dock; Supplier dock loading order; Plant code; Plant dock; Plant dock loading order; Product code; Arrival time; Id truck:Length:Width:Height:Max weight:Stack with multiple docks:Max density:Max weight on the bottom item in stacks:Cost:EMmm.EMmr:CM:CJfm:CJfc:CJfh:EM:EJhr:EJcr:EJeh 0062069400;1;;1;0090018000;x0;1;852480062B;202208182025;P230711301;14500;2400;2800;30000;0;1500;100000;1500;12000;31500;7808.000;3800;1040;3330;7300.000;7630;2350;1670 0062069400;1;;1;0090018000;X0;1;745322815R;202208182025;P230711301;14500;2400;2800;30000;0;1500;1500;12000;31500;7808,000;3800;1040;3330;7300,000;7630;2350;1670 0062069400;1;1;1;0090018000;X0;1;8201677103;202208182025;P230711301;14500;2400;2800;30000;0;1500;1500;12000;31500;7808,000;3800;1040;3330;7300,000;7630;2350;1670 062069400;1;;1;0090018000;X0;1;781419006B;202208182025;P230711301;14500;2400;2800;30000;0;1500;100000;1500;12000;31500;7808.000;3800;1040;3330;7300.000;7630;2350;1670 0620694001;;;;0090018000;X0;1;781405634B;202208182025;P230711301;14500;2400;2800;30000;0;1500;100000;1500;12000;31500;7808.000;3800;1040;3330;7300.000;7630;2350:1670 0062069400;1;;1;0090018000;X0;1;821474009R;202208182025;P230711301;14500;2400;2800;30000;0;1500;100000;1500;12000;31500;7808,000;3800;1040;3330;7300,000;7630;2350;1670 0062069400;1;1;1;0090018000;x0;1;766361764B;202208182025;P230711301;14500;2400;2800;30000;0;1500;1500;12000;31500;7808,000;3800;1040;3330;7300,000;7630;2350;1670 0062069400;1;;1:0090018000;x0;1;791407225R;202208182025;P230711301;14500;2400;2800;30000;0;1500;1500;12000;31500;7808.000;3800;1040;3330;7300.000;7630;2350;1670 0062069400;1;;1;0090018000;x0;1;776514302R;202208182025;P230711301;14500;2400;2800;30000;0;1500;1500;12000;31500;7808,000;3800;1040;3330;7300,000;7630;2350;1670 0062069400;1;1;1;0090018000;X0;1;745326954B;202208182025;P230711301;14500;2400;2800;30000;0;1500;1500;12000;31500;7808,000;3800;1040;3330;7300,000;7630;2350;1670 0062069400;1;;1:0090018000;x0;1;781400316R;202208182025;P230711301;14500;2400;2800;30000;0;1500;1500;12000;31500;7808.000;3800;1040;3330;7300.000;7630;2350;1670 0620694001:1:1:0090018000;X0:1:625191617B:202208182025;P230711301:14500:2400:2800:30000:0:1500:100000;1500:12000:31500:7808.000;3800:1040:3330:7300.000:7630:2350:1670 0620694001; ; ; ; 0090018000; x0; 1; 745338473B; 202208182025; P230711301; 14500; 2400; 2800; 30000; 0; 1500; 100000; 1500; 12000; 31500; 7808.000; 3800; 1040; 3330; 7300, 000; 7630; 2350; 1670 0062069400;1;;1;0090018000;x0;1;764558590R;202208182025;P230711301;14500;2400;2800;30000;0;1500;100000;1500;12000;31500;7808,000;3800;1040;3330;7300,000;7630;2350;1670 0062069400;1;;1;0090018000;x0;1;7641247578;202208182025; p230711301;14500;2400;2800;30000;0;1500;100000;1500;12000;31500;7808,000;3800;1040;3330;7300,000;7630;2350;1670 0062069400;1;1:0090018000;x0:1;781413811R;202208182025;P230711301;14500;2400;2800;30000;0;1500;1500;12000;31500;7808.000;3800;1040;3330;7300.000;7630;2350;1670 0620694001::1:0090018000;X0:1:656156707B:202208182025;P230711301:14500:2400:2800:30000:0:1500:100000;1500:12000:31500:7808.000;3800:1040:3330:7300.000:7630:2350:1670 0062069400:1::1:0090018000:x0:1:843408889p;202208182025:p230711301:14500:2400:2800:30000:0:1500:12000:31500:7808.000:3800:1040:3330:7300.000:7630:2350:1670 0062069400;1;1:10090018000;x0:1;763571615R;202208182025;P230711301;14500;2400;2800;30000;0;1500;1500;12000;31500;7808.000;3800;1040;3330;7300.000;7630;2350;1670 0620694001::1:0090018000;x0:1:8201677097:202208182025; P230711301:14500:2400:2800:30000:0:1500:100000:1500:12000:31500:7808.000:3800:1040:3330:7300.000:7630:2350:1670 0620694001::1:0090018000;x0:1:732567222B:202208182025;P230711301:14500:2400:2800:30000:0:1500:100000;1500:12000:31500:7808.000:3800:1040:3330:7300.000:7630:2350:1670 0620694001::1:0090018000;x0:1:8201560251:202208182025; P230711301:14500:2400:2800:30000:0:1500:100000; 1500:12000:31500:7808.000:3800:1040:3330:7300.000:7630:2350:1670 0620694001::1:0090018000;x0:1:764547307B:202208182025;P230711301:14500:2400:2800:30000:0:1500:100000:1500:12000:31500:7808.000:3800:1040:3330:7300.000:7630:2350:1670 0620694001::1:0090018000;x0:1:7653777598:202208182025:P230711301:14500:2400:2800:30000:0:1500:100000:1500:12000:31500:7808.000:3800:1040:3330:7300.000:7630:2350:1670 0062069400:1::1:0090018000:x0:1:8524862878:202208182025:p230711301:14500:2400:2800:30000:0:1500:1500:12000:31500:7808.000:3800:1040:3330:7300.000:7630:2350:1670 062069400:1::1:0090018000;x0:1:8201745175:202208182025:p230711301:14500:2400:2800:30000:0:1500:100000:1500:12000:31500:7808.000:3800:1040:3330:7300.000:7630:2350:1670 0620694001::1:0090018000;x0:1:7624284808:202208182025:p230711301:14500:2400:2800:30000:0:1500:100000:1500:12000:31500:7808.000:3800:1040:3330:7300.000:7630:2350:1670 0062069400;1;;1;0090018000;X0;1;762432908R;202208182025;P230711301;14500;2400;2800;30000;0;1500;100000;1500;12000;31500;7808,000;3800;1040;3330;7300,000;7630;2350;1670



Realistic Examples

## Input Data (II)

### Items to be Transported

Item ident; Supplier code; Supplier dock; Plant code; Plant dock; Product code; Package code; Number of items; Length; Width; Height; Weight; Nesting height; Stackability code; Forced orientation; Earliest arrival time; Latest arrival time; Inventory cost; Max stackability 0090018000 03072022000001:0062069400::0090018000:X0:762432908R:CON-8-0130:3:780:570:478:81.720:47:GERB--3195 780 570:widthwise:202208190000:20220822025:2:4 0990018000 03072022000002:0062069400;:0090018000;x0;6636065008:CON-S-0130;3;780;570;478;96,256;47;GERB--3195 780 570;widthwise:202207200000;202207212025;3;4 0090018000 03072022000003;0029918200;;0090018000;x1;550206080R;8LI---0770;6;1200;1000;975;577,800;45;GERB--1213 1200 1000;none;202207130000;202207140603;7;100 0090018000 03072022000004:0028091900::0090018000:x4:403007072R:EN8---0014:10:1400:1225:1160:278.500:0:GERB--7976 1400 1225:none:202208250000:202208261400:15:100 0090018000 03072022000005;0062069400;;0090018000;X0;745326954R;CON-s-0130;5;780;570;478;100,960;47;GERB--3195 780 570;widthwise;202207080000;202207112025;1;4 0090018000 03072022000006;0029938000;;0090018000;X3;2727044638;ECM---5565;16;1400;1200;1450;179,400;45;GERB--0475 1400 1200;none;202208230000;202208241020;10;100 0090018000 03072022000007;0062069400;:0090018000;x0;852480062R;8LI---1271;1;1600;1200;975;1471.600;45;GERB--1613 1600 1200;none:202207130000;202207142025;26;100 0090018000 03072022000008;0062069400;;0090018000;x0;764131108B;SLI---1101;1;1900;1200;750;713,620;45;GEBB--0109 1900 1200;none;202208100000;202208112025;13;100 0990018000 03072022000009;0029938000;:0090018000;x3;272707927R;ECM---5565;12;1400;1200;1450;179.400;45;GERB--0475 1400 1200;none;202208080000;202208091020;10;100 0090018000 0307202200010;0062060800;;0090018000;x2;172022957R;ECM---0559;8;1600;1200;1350;303,920;45;GERB--1613 1600 1200;none;202208010000;202208021800;5;100 0090018000 03072022000011:0028091900::0090018000:x4:403008854B:ENS---0015:11:1400:1225:1160:317.000:0:GERB--7976 1400 1225:none:202207190000:202207201400:16:100 0090018000 0307202200012:0062069400::0090018000:x0:763571615B:BLI---0601:1:1200:1000:750:227.528:45;GERB--1213 1200 1000:none:202208190000:20220822025:5:100 0090018000 03072022000013;0062069400;;0090018000;x0;901323145R;CON=s=0130;1;780;570;478;101,520;47;GERB==3195 780 570;widthwise;202208170000;202208182025;3;4 0090018000 03072022000014;0062069400;:0090018000;x0;625189279R; CON-s-0130;1;780;570;478;270,080;47;GERB--3195 780 570;widthwise:202208050000;202208082025;6;4 0090018000 03072022000015,0025439300;:0090018000;x0;8021024638;5LI---1200;3;1600;1200;930;454.873;45;GERB--1613 1600 1200;none:202208190000;202208221735;8:100 0090018000 03072022000016;0062069400;;0090018000;X0;8201677033;8LI--1200;3;1600;1200;930;547.300;45;GERB--1613 1600 1200;none;202207290000;202208012025;1:100 0090018000 03072022000017:0062060800::0090018000:X2:172039318R;ECM---0559:6:1600:1200:1350:303.920:45:GERB--1613 1600 1200:none:202208170000:202208181430:5:100 0090018000 03072022000018:0062069400::0090018000:X0:8201677033:8T.T---1200:4:1600:1200:930:547.300:45:GEBB--1613 1600 1200:none:202207130000:202207142025:1:100 0090018000 03072022000019;0062060800;;0090018000;x2;172039318R;ECM---0559;2;1600;1200;1350;303,920;45;GERB--1613 1600 1200;none;202207260000;202207271800;5;100 0090018000 03072022000020;0002893800;;0090018000;x1;769235146R;SLI---0770;1;1200;1000;975;246,000;45;GERB--1213 1200 1000;none;202207220000;202207251600;4;100 0090018000 03072022000021;0062069400;:0090018000;x0;8201677103;ECM---1934;2;1200;1000;545;729.500;45;GERB--1213 1200 1000;none:202207180000;202207192025;2;100 0090018000 03072022000022:0062060800;:0090018000;x2:172022957R; ECM---0559:1:1600:1200:1350:303.920:45; GERB--1613 1600 1200:none:202208080000:202208091430:5:100 090018000 03072022000023:0062069400::0090018000:x0:7765073888:5L1---0601:3:1200:1000:750:229.880:45;GERB--1213 1200 1000:none:202208260000:202208292025:4:100 0090018000 03072022000024;0062069400;:0090018000;x0;8201590963;CON-8=0130;1;780;570;478;160,560;47;GERB==3195 780 570;widthwise;202208050000;202208082025;1;4 0090018000 03072022000025;0029938000;:0090018000;x3;2727044638;ECM---5565;12;1400;1200;1450;179.400;45;GERB--0475 1400 1200;none;202207220000;202207251020:10:100 0090018000 03072022000026;0062069400;:0090018000;x0;625191617R;CON-8-0130;11780;570;478;269.320;47;GERB-3195 780 570;widthwise;202207180000;202207192025;6;4 0090018000 03072022000027;0062060800;;0090018000;x2;172022957R;ECM---0559;7;1600;1200;1350;303,920;45;GERB--1613 1600 1200;none;202207150000;202207180915;5;100

### Parameters of Problem

1 Coefficient inventory cost; Coefficient transportation cost; Coefficient cost extra truck; timelimit (sec)

2 10;1;0,2;1800

3

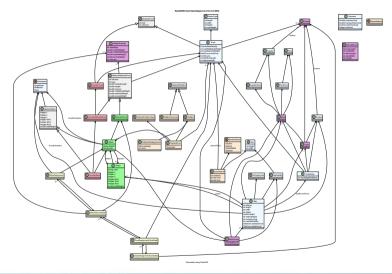


## **Observations**

- Data size varies between instances, but is typically (very) large
- Four stages of data availability, 150 instances in total
- One sample solution given
- But: Checker (in java) provided, normative
- Problem description 11+8 pages
- Data tables not normalized, contains much redundant information
- Normalizing data leads to UML Object Model on next slide



## **Resulting Object Model**





Realistic Examples

## **Defined Output Format**

## • Three files

- Trucks used
- Stacks built
- Pieces placed
- No direct link between planned and scheduled trucks
- Concept of stack is redundant
- One item results in multiple pieces
- Link between trucks, stacks, pieces and input data by string ids

Id truck	char	P380411201	
Loaded length	int	12500  mm	$max_{s \in \widetilde{TS}_{s}} sx_{s}^{e}$
Weight of loaded items	float	1894,31	kg
Volume of loaded items	float	14,544	$m^3$
Weight on the middle axle of the trailer $(em^m)$	float	1875,83	kg
Weight on the rear axle of the trailer $(em^r)$	float	18,47	kg

Field	Type	Example	Comments
Id truck	char	P380411201	Must be defined in the output trucks file
Id stack	char	P380411201_1	
Stack code	char	Α	To be used for display (cf FIGURE 1)
X origin $(sx_s^o)$	int	0	mm
Y origin $(sy_s^o)$	int	0	mm
Z origin $(sz_s^o)$	int	0	mm
X extremity $(sx_s^e)$	int	1010	mm
Y extremity $(sy_s^e)$	int	1206	mm
Z extremity $(sz_s^e)$	int	407	mm

Field	Type	Example	Comments
Item ident	char	$00900160_{20221201_{2314}}$	Must be defined in the input items file
Id truck	char	P380411201	Must be defined in the output trucks file
Id stack	char	P380411201_1	Must be defined in the output stacks file
Item code	char	A1	To be used for display (cf FIGURE 1)
X origin	int	0	mm
Y origin	int	0	mm
Z origin	int	0	mm
X extremity	int	1010	mm
Y extremity	int	1206	mm
Z extremity	int	407	mm

## **Complex Side Constraints**

 Some of the constraints are not just simple, linear formulas

$$ej^e = \frac{\sum_{s \in \widetilde{TS}_t} (sx^o_s + \frac{(sx^e_s - sx^o_s)}{2}) \times sm_s}{tm_t}$$

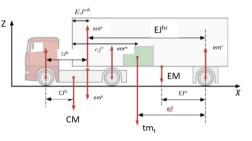
$$ej^r = EJ^{eh} + EJ^{hr}$$
 -  $ej^e$ 

$$em^h = \frac{tm_t \times ej^r + EM \times EJ^{cr}}{EJ^{hr}}$$

$$em^r = tm_t + EM$$
 -  $em^h$ 

$$em^m = \frac{CM \times CJ^{fc} + em^h \times CJ^{fh}}{CJ^{fm}}$$

• Interpretation requires detailed physical model





## A Grand Challenge for Constraint Acquisition

- Can you extract a transferable model of this problem?
  - Given the data and solutions of all problem instances
- Not too hard to find packing constraints for pieces
- Packing constraints for stacks are simple
- Real problem
  - How many stacks are needed?
  - How many trucks are needed?
  - Many non-trivial side constraints!
- Previous competitions provide similar challenges
  - There is a checker!
  - Lots of instances
  - Solutions not known until challenge end



## An Industrial Example

- ASSISTANT Siemens Energy use case
- Mid/Long-term scheduling/production planning
- Realistic/not real data
- Rather complex constraint model
  - Multi-stage BOM
  - Alternative Process Paths
  - Alternative machines
  - Quality/cost based routing preferences
  - Potential outsourcing of certain steps
  - Machine specific calendars
  - Infeasible release/due date pairs
  - Calendar dependent speed reduction
  - Complex manpower constraints



## Assistant Siemens Energy Use Case



### **Use Case Scenarios**

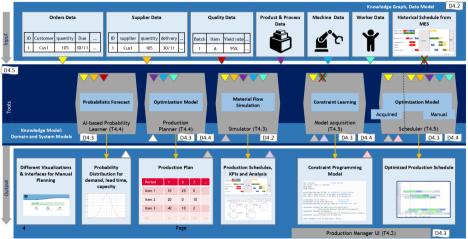
- Schedule *validation* of gas turbine blades and vanes manufacturing operations in Berlin plant
- Schedule *optimization* to manage short-term, mid-term and long-term load fluctuations
- Generate Make-or-Buy proposals for workload balancing within the manufacturing network



## **Digital Twin**

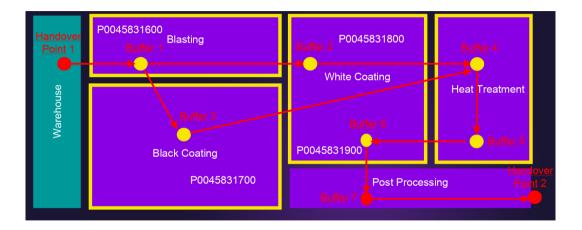
### Intelligent digital twin for process planning and scheduling







## **SE Product Routing**





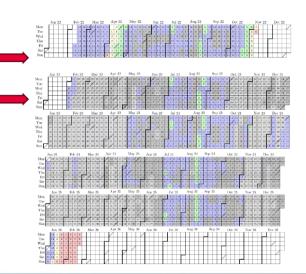
Realistic Examples

**Datasets** 

## Full Scale Datasets

Berlin06: 96 orders, 9 months horizon, previous review Berlin07: 450 orders, 4 years horizon Berlin08: 559 orders, Christmas gap added Berlin08a: 670 orders, filling gaps

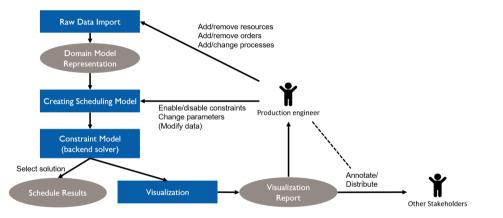
Value in cell indicates active orders Yellow and red colors indicate low order volume





Realistic Examples

## **Optimizer High Level Structure**





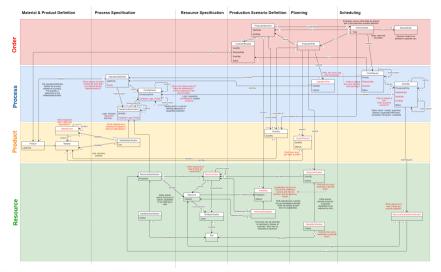
## Raw Data - Manual Data Entry Causes Problems

- Raw data come from spreadsheet
  - 20 tabs
- Excel is a particularly bad input data format
- Realistic, not real data
- Created by hand/automatically from existing test scenarios
- Series of files Berlin01 Berlin05 were too inconsistent to run
- Berlin06 still contains some errors
- Optimizer explains all issues that it finds

		rio View Wind				
lawlanus						
Name	Severity	Sheet	RowNr	ColNr	Description	
Issue1	Major	tLoad	129	11	DateTime not formatted correctly, found 2022-02-2800:00:00 format yyyy-MM-dd/THH:mmas	
Issue2	Minor	€Products			Extra Empty Header	
Issue3	Minor	(Availabilities	1	8	Extra Empty Header	
Issue4	Minor	t_Unavailabilities		8	Extra Empty Header	
Issue5	Minor	CShift_Segments	1	6	Extra Errpty Header	
Issue6	Major	LShift_Segments	1	1	TimeOnly not formatted correctly, found 0.250000, format Hommas	
Issue?	Major	LShill_Segments	1	2	TimeOnly not formatted correctly, found 0.583333, format Hommas	
Issue8	Major	LShill_Segments	2	1	TimeOnly not formatted correctly, found 0.291667, format Hommas	
Issoe	Major	CShift_Segments	2	2	TimeOnly not formatted correctly, found 0.302083, format Hommiss	
Issue10	Major	LShift_Segments	3	1	TimeOnly not formatted correctly, found 0.458333, format Hommiss	
Issue11	Major	UShi/USegments	3	2	TimeOnly not formatted correctly, found 0.479167, format Hummiss	
Issue12	Major	LShift_Segments	- 4	1	TimeOnly not formatted correctly, found 0.583333, format Himmiss	
Issue13	Major	UShi/USegments	4	2	TimeOnly not formatted correctly, found 0.916667, format Hummiss	
Issue14	Major	LShift_Segments	5	1	TimeOnly not formatted correctly, found 0.666667, format Hommas	
ssue15	Major	LShift_Segments	5	2	TimeOnly not formatted correctly, found 0.677083, format Hommas	
Issue16	Major	LShift_Segments	6	1	TimeOnly not formatted correctly, found 0.770833, format Hommiss	
Issue17	Major	LShift_Segments	6	2	TimeOnly not formatted correctly, found 0.791667, format Hommas	
Issue18	Major	LShift_Segments	7	1	TimeOnly not formatted correctly, found 0.916667, format Hommas	
Issue19	Major	LShift_Segments	7	2	TimeOnly not formatted correctly, found 0.250000, format Hummas	
ssue20	Major	LShift_Segments	8	1	TimeOnly not formatted correctly, found 0.000000, format Hommas	
ssue21	Major	CShift_Segments	8	2	TimeOnly not formatted correctly, found 0.010417, format Hommiss	
Issue22	Major	LShift_Segments	9	1	TimeOnly not formatted correctly, found 0.083333, format Himmiss	
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Issue26	Minor	LShift_Segments	12	0	First Column Empty	
s91e27	Minor	t_Shift_Segments	13	0	First Column Empty	
s91e28	Minor	t_Shift_Segments	14	0	First Column Empty	
s91e29	Minor	t_Shift_Segments	15	0	First Column Empty	
ssue30	Minor	t_Shift_Segments	16	0	First Column Empty	
ssue31	Minor	t_Shift_Segments	17	0	First Column Empty	
s91e32	Minor	t_Shift_Segments	18	0	First Column Empty	
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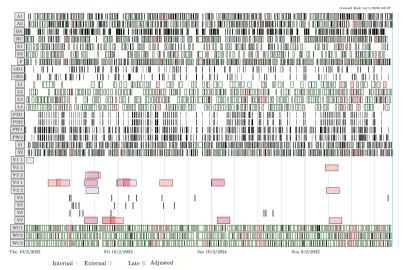


## Domain Model - Knowledge Graph





## Single Solution for Berlin 08a - Shows Only 20% of Tasks in Model



Insight

#### Realistic Examples

## Challenges for CA

- Input data not fully consistent
- Decide what to do with detected problems
- Solution only shows active part of schedule
- Large set of optional tasks not visible as not active
- Input data contain many fields which are irrelevant for scheduler
  - Component level information
  - Nomenclature
- Many task properties are computed from input data
  - Understand links between multiple objects
  - Time resolution/rounding



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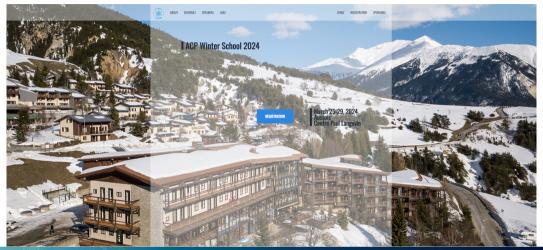


- Presented different sources for CA benchmarks from simple to complex
- Few sources present all elements required for CA
- Benchmarks rather than competition
- Why data format is important
- As authors, please provide data, solutions, checkers
- Algorithms are necessary, but not sufficient for Constraint Acquisition



## Ad: ACP Winter School 2024

### • March 25-29, Aussois, France, https://school.a4cp.org/winter2024/





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